

8-1 Factors and Greatest Common Factors

□ **FACTORS:** a number or numbers that are multiplied together to get a product.

$$\begin{array}{ccc} 3 * 4 = 12 \\ \vee \quad \quad \quad \vee \\ \text{factors} \quad \quad \text{product} \end{array}$$

□ **GREATEST COMMON FACTOR (GCF):** the biggest factor found in all factors for each number, monomial, or expression.

15: 1, 3, 5, 15

18: 1, 2, 3, 6, 9, 18

The GCF of 15 and 18 is 3.

Examples:

Find the GCF of each pair of numbers

1) 12 and 24

12: 1, 2, 3, 4, 6, 12 12

2) 15 and 40

15: 1, 3, 5, 15 5

24: 1, 2, 3, 4, 6, 8, 12, 24

40: 1, 2, 4, 5, 8, 10, 20, 40

3) 36 and 48

36: 1, 2, 3, 4, 6, 9, 12, 18, 36 12

48: 1, 2, 3, 4, 6, 8, 12, 16, 24, 48

□ FINDING THE GCF OF MONOMIALS

4) $12y$ and $15y^2$

$12y$: 1, 2, 3, 4, 6, 12, y

$15y^2$: 1, 3, 5, 15, y, y

$3y$

5) $3p^4$ and $2p^2$

$3p^4$: 1, 3, p, p, p, p

$2p^2$: 1, 2, p, p

$p^2 \rightarrow p^2$

6) $14xy^2$ and $21xy^3$

$14xy^2$: 1, 2, 7, 14, x, y, y

$21xy^3$: 1, 3, 7, 21, x, y, y, y

$7xy^2$

□ FINDING THE GCF OF EXPRESSIONS

7) $5(x-3)$ and $25(x-3)^3$

$5(x-3)$: 1, 5, $(x-3)$

$25(x-3)^3$: 1, 5, 25, $(x-3), (x-3), (x-3)$

$5(x-3)$

8) $12(a-4)^5$ and $2(a-4)^4$

$12(a-4)^5$: 1, 2, 3, 4, 6, 12, $(a-4), (a-4), (a-4), (a-4), (a-4)$

$2(a-4)^4$: 1, 2, $(a-4), (a-4), (a-4), (a-4)$

$2(a-4)^4$

9) $-7(z-9)^8$ and $14(z-9)^2$

$-7(z-9)^8$: -1, 1, -7, $(z-9), (z-9), (z-9), (z-9), (z-9), (z-9), (z-9), (z-9)$

$14(z-9)^2$: 1, 2, 7, 14, $(z-9), (z-9)$

$7(z-9)^2$